

# Design of RF-Choke Inductors Using Core Geometry Coefficient

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**Abstract**—This paper presents a derivation of the core geometry coefficient  $K_g$  for the design of RF-choke inductors and a design example. The design example indicates that the dc winding loss is the dominant component of the total power loss of RF-choke inductors. Additionally, the advantages and disadvantages of the  $K_g$  method are discussed by using the design example results.

**Index Terms**—Inductor design, RF-choke inductor, core geometry coefficient, dc winding loss, ac winding loss, core loss, air-gap length, fringing effect, skin effect, Dowell's equation.

## INTRODUCTION

The magnetic component design is a traditional problem, but it is not solved satisfactorily in the power electronics field. For example, the RF-power amplifier, which is one of the important circuits in many systems, has two major magnetic components: a resonant inductor and an RF-choke inductor. In particular, most of the RF-power amplifiers, which are the class A, class B, class AB, class C, class E, and class F amplifiers, have an RF-choke inductor [1]. The improvements of some kinds of switching techniques, e.g., zero-voltage switching (ZVS), zero-current switching (ZCS), and class-E ZVS and zero derivative switching (ZDS), reduce dramatically power losses in switching devices. Therefore, the importance of the design of magnetic components with low power losses increases for the design of power amplifiers and dc-dc converters. Additionally, the reduction of the magnetic-component volume is also an important aspect because the magnetic components are bottlenecked to determine the circuit size. Generally, the power loss in a magnetic component decreases when the size of the inductor increases though both the low power loss and small volume are required. This means that there is a trade-off relationship between the power loss and the magnetic component size. Therefore, the design of magnetic components, which are inductors and transformers, is one of the important challenging problems.

There are several well-known strategies for selecting a core for the design of magnetic components, for example, the area product ( $A_p$ ) method and the core geometry ( $K_g$ ) method [2]–[5]. These methods are primarily used in the design of inductors and transformers for switching-mode power supplies (SMPS). The concept of the  $A_p$  approach is to select a proper

core satisfying both the electromagnetic conditions and the restriction of the core window area. The inductance value is adjusted by the air-gap length. The  $A_p$  method is widely used for designing the inductors and transformers for dc-dc power converters operating in CCM and DCM. On the other hand, the concept of the  $K_g$  approach is to select a proper core satisfying the electromagnetic conditions, the restriction of the core window area, and the restriction of the winding loss, simultaneously. This method is useful to design inductors and transformers with low core and low ac winding losses. By setting the dc winding loss, we can choose the core, which requires shorter length and narrower cross-sectional area of the wire compared to that obtained with the  $A_p$  method. This leads to a small core volume.

An RF-choke inductor forces a dc current, which is applicable to dc-current sources and output filters of resonant converters. Since the current through the RF-choke inductor includes a low ac component, the ac-winding loss and the core loss are very small, even if the operating frequency is high. Therefore, it is possible to focus on the dc-winding loss when the RF-choke inductor is designed. Additionally, the inductance value of the RF choke inductor is usually high to force the dc current. Therefore, the volume reduction is quite important to make an RF-choke inductor. For the reasons described above, we consider that the  $K_g$  method is suitable to design the RF-choke inductor.

This paper presents a derivation of the core geometry coefficients  $K_g$  for the design of the RF-choke inductors and a design example. The design example indicates that the dc winding loss is dominant in the power losses of the RF-choke inductor. Additionally, the advantages and disadvantages of the  $K_g$  method are discussed by using the design example results.

## I. BASIC THEORY AND DERIVATION OF CORE GEOMETRY COEFFICIENT $K_g$

### A. Expression for Current Through RF-Choke Inductor

The purpose of a choke is to supply a dc current. In real circuits, however, there are a little ripple on the dc current. Therefore, we assume that the current through the inductor  $i_L$  is the sum of a direct current  $I_{dc}$  and a pure sinusoidal current with the fundamental frequency equal to the operating

frequency  $f$ ,

$$i_L = I_{dc} + \frac{I_{pp}}{2} \sin(\omega t) = I_{dc} + (I_m - I_{dc}) \sin(\omega t), \quad (1)$$

where  $I_{pp}$  is peak-to-peak value of the ac component of the current,  $I_m$  is a maximum value of  $i_L$  and  $\omega = 2\pi f$  is the angular frequency. In this case, the peak-to-peak ripple ratio to the dc current through the inductor is defined as

$$\gamma_r \equiv \frac{\Delta i_L}{I_{dc}} = \frac{I_{pp}}{I_{dc}} = \frac{2(I_m - I_{dc})}{I_{dc}}. \quad (2)$$

### B. Core Geometry Coefficient $K_g$ for RF-Choke Inductors

The inductance of an inductor with an air gap is given by

$$L = \frac{N^2}{\frac{l_g}{\mu_0 A_c} + \frac{l_c}{\mu_r \mu_0 A_c}} = \frac{\mu_0 N^2 A_c}{l_g + \frac{l_c}{\mu_r}}, \quad (3)$$

where  $N$  is the number of wire turns,  $l_g$  is the air-gap length,  $l_c$  is the core length,  $A_c$  is the cross-sectional area of the magnetic core,  $\mu_0 = 4\pi \times 10^{-7}$  H/m is the free-space permeability, and  $\mu_r$  is the relative permeability of the core material.

In general, it can be written that

$$Ni = B \left( \frac{l_g}{\mu_0} + \frac{l_c}{\mu_0 \mu_r} \right), \quad (4)$$

where  $B$  is the flux density. Hence, the maximum flux density  $B_m$  is

$$B_m = \frac{\mu_0 N I_m}{\frac{l_c}{\mu_r} + l_g} = \frac{\mu_0 N I_{dc} (1 + \gamma_r/2)}{\frac{l_c}{\mu_r} + l_g}. \quad (5)$$

From (3) and (5), the number of turns is

$$N = \frac{L I_m}{A_c B_m} = \frac{L I_{dc} (1 + \gamma/2)}{A_c B_m}, \quad (6)$$

which is obtained from electromagnetic point of view. The length of the winding wire is

$$l_w = N l_T, \quad (7)$$

where  $l_T$  is the mean length of a single turn (MLT). The dc winding resistance is

$$R_{wdc} = \frac{\rho_w l_w}{A_w} = \frac{\rho_w N l_T}{A_w}, \quad (8)$$

where  $A_w$  and  $\rho_w$  are the cross-sectional area of the winding bare wire and the resistivity of the copper, respectively. Therefore,

$$A_w = \frac{N \rho_w l_T}{R_{wdc}}. \quad (9)$$

The dc winding loss is

$$P_{wdc} = R_{wdc} I_{dc}^2. \quad (10)$$

Therefore, (9) is rewritten as

$$A_w = \frac{N \rho_w l_T I_{dc}^2}{P_{wdc}}. \quad (11)$$

Designed Inductor

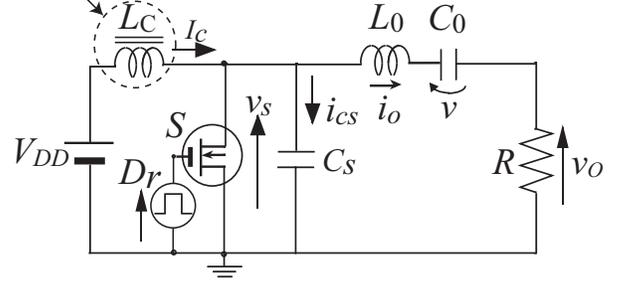


Fig. 1. Circuit topology of the class E amplifier.

The core window utilization factor is defined as the ratio of the total cross-sectional area of the winding bare wire  $A_{Cu}$  to the window cross-sectional area of a core  $W_a$

$$K_u = \frac{A_{Cu}}{W_a} = \frac{N A_w}{W_a}. \quad (12)$$

From (11) and (12), we obtain

$$N^2 = \frac{K_u W_a P_{wdc}}{\rho_w l_T I_{dc}^2} \quad (13)$$

and

$$A_w^2 = \frac{K_u W_a \rho_w l_T I_{dc}^2}{P_{wdc}}. \quad (14)$$

These relations include both the dc winding loss condition in (11) and core-area condition in (12). The number of turns should also satisfy the electromagnetic condition in (6). Equating of the right-hand sides of (6) and (13), the *core geometry coefficient* [2] is obtained as

$$\begin{aligned} K_g &= \frac{W_a A_c^2 K_u}{l_T} \\ &= \frac{\rho_w L^2 I_m^2 I_{dc}^2}{P_{wdc} B_m^2} = \frac{\rho_w L^2 I_{dc}^4 (1 + \gamma/2)^2}{P_{wdc} B_m^2} \quad (\text{m}^5), \end{aligned} \quad (15)$$

It is convenient to express the dc winding loss as the ratio of the output power  $P_{wdc} = \alpha P_o$ , resulting

$$K_g = \frac{\rho_w L^2 I_m^2 I_{dc}^2}{\alpha P_o B_m^2} = \frac{2 \rho_w L I_{dc}^4 (1 + \gamma/2)^2}{\alpha P_o B_m^2}. \quad (16)$$

The core geometry coefficient  $K_g$  provides the core with a good combination of  $W_a$ ,  $A_c$ , and  $l_T$  satisfying electromagnetic condition in (9), dc-winding-loss condition in (11), and core-area restriction in (12), simultaneously. The concrete values of  $K_g$  are presented for  $K_u = 0.4$  in [3], or can be calculated from the core dimensions provided by the core manufacturers. By using the proposed expressions for  $K_g$  in (15) and (16), we can select the core satisfying the conditions (9), (11), and (12) using only the electrical parameters.

## II. DESIGN EXAMPLE

### A. Design Specifications and Conditions

This section presents a design example of an RF-choke inductor for the class-E resonant power amplifier [6] whose topology is shown in Fig. 1. The specifications of the class-E amplifier are: operating frequency  $f = 1$  MHz, load resistance  $R_L = 10 \Omega$ , loaded quality factor  $Q_L = 5$ , and supply voltage  $V_{DD} = 15$  V. By using the design procedure in [6], the inductance value of the RF-choke to achieve the ripple ratio  $\gamma_r = 1$  % is  $L_c = 1.13$  mH. In this case, the dc-current and the maximum current through the inductor is  $I_{dc} = 0.807$  A and  $I_m = I_{dc}(1 + \gamma_r/2) = 0.811$  A. The output power is  $P_o = 11.8$  W.

The RF-choke inductor is designed to achieve the following specifications: 1) maximum current density of the wire is  $J_m < 5$  A/m<sup>2</sup>, 2) core window utilization factor is  $K_u = 0.4$ , 3) maximum flux density is less than the saturated flux density,  $B_m < B_{sat} = 0.5$  T, and 4) dc-winding-loss coefficient is  $\alpha = 0.005$ .

### B. Core Geometry Factor and Core Selection

From (16), the core geometry coefficient is obtained as

$$\begin{aligned} K_g &= \frac{\rho_w L_c^2 I_{dc}^4 (1 + \gamma_r/2)^2}{\alpha P_o B_m^2} \\ &= \frac{1.72 \times 10^{-7} \times 1.13 \times 10^{-3}}{0.005 \times 11.8 \times 0.3^2} \\ &\quad \times 0.807^4 \times (1 + 0.01/2)^2 \\ &= 1.768 \times 10^{-12} \text{ m}^5. \end{aligned} \quad (17)$$

We select Magnetic PQ-42020 core with the R ferrite material whose parameters are [3]:  $\mu_r = 2300$ ,  $K_g = 1.859 \times 10^{-12} \text{ m}^5$ ,  $A_c = 0.58 \text{ cm}^2$ ,  $W_a = 0.6 \text{ cm}^2$ ,  $l_T = 4.3 \text{ cm}$ ,  $l_c = 4.5 \text{ cm}$ , height of core window  $g = 1.4 \text{ cm}$ , and core volume  $V_c = 2.61 \text{ cm}^3$ .

### C. Wire Selection

From (14), the cross-sectional area of the bare wire is given by

$$\begin{aligned} A_w &= \sqrt{\frac{K_u W_a \rho_w l_T I_{dc}^2}{\alpha P_o}} \\ &= \sqrt{\frac{0.4 \times 0.6 \times 10^{-4} \times 1.72 \times 10^{-8}}{0.005 \times 11.8}} \\ &\quad \times \sqrt{4.5 \times 10^{-2} \times 0.807^2} \text{ (m}^2\text{)} \\ &= 0.442 \text{ mm}^2. \end{aligned} \quad (18)$$

From  $A_w$ , we pick the AWG 20 copper wire with  $A_w = 0.519 \text{ mm}^2$ , inner diameter of bare wire cross-sectional area  $d_i = 0.812 \text{ mm}$ , and outer diameter including insulation  $d_o =$

0.879 mm. The maximum current density of the wire is

$$\begin{aligned} J_m &= \frac{I_{dc}(1 + \gamma_r/2)}{A_w} \\ &= \frac{0.807 \times (1 + 0.01/2)}{0.518 \times 10^{-6}} \\ &= 1.56 \text{ A/m}^2 < 5. \end{aligned} \quad (19)$$

It is confirmed that the wire satisfies the maximum-current-density condition. In the inductor design using the core geometry coefficient, the maximum-current-density condition is not guaranteed. Therefore, we need to confirm this condition. From (12), the number of turns is

$$N = \frac{K_u W_a}{A_w} = \frac{0.4 \times 0.6 \times 10^{-4}}{0.518 \times 10^{-6}} = 46.2. \quad (20)$$

We pick  $N = 46$ .

### D. Air-Gap Length Considered with Fringing Effect

For the adjustment of the inductance  $L_0$ , the air-gap length is calculated as

$$\begin{aligned} l_g &= \frac{\mu_0 A_c N^2}{L_0} - \frac{l_c}{\mu_r} \\ &= \frac{4 \times \pi \times 10^{-7} \times 0.58 \times 10^{-4} \times 46^2}{1.13 \times 10^{-3}} \\ &\quad - \frac{4.5 \times 10^{-2}}{2300} \text{ (m)} \\ &= 0.121 \text{ mm}. \end{aligned} \quad (21)$$

We shall choose a standard value of the air-gap length  $l_g = 0.1 \text{ mm}$ . Here, we consider the fringing effect. The fundamental theory of the fringing effect is given in [4]. In this design example, we assume the ratio of the effective width of the fringing flux cross-sectional area to the gap length as  $u = 1$ . In this case, the fringing area  $A_f$  is

$$\begin{aligned} A_f &= \pi u l_g (2\sqrt{A_c/\pi} + u l_g) \\ &= \pi \times 1 \times 0.1 \times 10^{-3} \\ &\quad \times (2 \times \sqrt{0.58 \times 10^{-4}/\pi} + 1 \times 0.1 \times 10^{-3}) \\ &= 0.0288 \text{ cm}^2. \end{aligned} \quad (22)$$

It is assumed that the ratio of the effective magnetic path length of the fringing flux to the gap length  $k = 2$ . Therefore, the fringing factor  $F_f$  is obtained as

$$\begin{aligned} F_f &= 1 + \frac{A_f}{A_c k} \\ &= 1 + \frac{0.0288 \times 10^{-6}}{0.58 \times 10^{-6} \times 2} = 1.02. \end{aligned} \quad (23)$$

The number of turns  $N = 46$  should be kept for achieving the specified  $K_u$  and  $B_m$ . Therefore, The estimated value of the

inductance  $L_c$  is

$$\begin{aligned} L_c &= \frac{\mu_0 A_c N^2}{l_g/F_f + l_c/\mu_r} \\ &= \frac{4 \times \pi \times 10^{-7} \times 0.58 \times 10^{-4} \times 46^2}{0.1 \times 10^{-3}/1.02 + 2.13 \times 10^{-3}/2300} \\ &= 1.33 \text{ mH}, \end{aligned} \quad (24)$$

where  $L_0$  is 18 % larger than the specified inductance. This difference appears due to the use of the standard length value of the air gap. The purpose of RF-choke inductor is to obtain the dc-current. Therefore large value of  $L_c$  is not problem for applying to the class-E switching amplifier.

### E. Power Loss Estimation

From the height of the core, we can obtain the maximum number of turns per one winding layer  $N'$

$$\begin{aligned} N' &= \frac{g}{d_o} \\ &= \frac{1.4 \times 10^{-2}}{0.879 \times 10^{-3}} = 15.9 \text{ turns/layer}. \end{aligned} \quad (25)$$

Therefore, 15 turns are allowed per one winding layer. The number of the winding layer  $N_l$  is

$$\begin{aligned} N_l &= \frac{N}{N'} \\ &= \frac{46}{15} = 3.06. \end{aligned} \quad (26)$$

Strictly speaking, we need 4-layer windings to realize the inductor. But 4th layer is only one turn. Therefore, we use  $N_l = 3$  to estimate the winding loss. The length of the winding wire is

$$\begin{aligned} l_w &= N l_T \\ &= 46 \times 4.3 \times 10^{-2} = 1.98 \text{ m}. \end{aligned} \quad (27)$$

The dc winding resistance is

$$\begin{aligned} R_{wdc} &= \frac{\rho_w l_w}{A_w} \\ &= \frac{1.72 \times 10^{-8} \times 1.02}{\pi \times 0.518 \times 10^{-6}} (\Omega) = 62.5 \text{ m}\Omega, \end{aligned} \quad (28)$$

where  $\rho_w = 1.72 \times 10^{-8} \Omega\text{m}$  is the resistivity of the copper at  $T = 20^\circ\text{C}$ . The dc winding power loss is

$$\begin{aligned} P_{wdc} &= R_{wdc} I_{dc}^2 \\ &= 62.5 \times 10^{-3} \times 0.807^2 (\text{W}) = 50.2 \text{ mW}. \end{aligned} \quad (29)$$

The skin depth of copper at  $f = 1 \text{ MHz}$  is,

$$\begin{aligned} \delta_w &= \frac{\rho_w}{\pi \mu_0 f} \\ &= \sqrt{\frac{1.724 \times 10^{-8}}{\pi \times 4 \times \pi \times 10^{-7} \times 10^6}} (\text{m}) \\ &= 66.0 \text{ }\mu\text{m}. \end{aligned} \quad (30)$$

The porosity factor  $\eta_p$  is

$$\begin{aligned} \eta_p &= \frac{d_o N}{g N_l} \\ &= \frac{0.879 \times 10^{-3} \times 46}{1.4 \times 10^{-2} \times 3} = 0.94. \end{aligned} \quad (31)$$

We estimate the ac winding loss using Dowell's equation [4]. The factor of Dowell's equation for round wire is

$$\begin{aligned} A &= \left(\frac{\pi}{4}\right)^{\frac{3}{4}} \frac{d}{\delta_w} \sqrt{\eta_p} \\ &= \left(\frac{\pi}{4}\right)^{\frac{3}{4}} \times \frac{0.879 \times 10^{-3}}{66 \times 10^{-6}} \times \sqrt{0.94} = 10.8. \end{aligned} \quad (32)$$

By using the factor  $A$ , we obtain the winding ac-to-dc resistance ratio is

$$\begin{aligned} F_R &= A \left[ \frac{\sinh(2A) + \sin(2A)}{\cosh(2A) - \cos(2A)} \right. \\ &\quad \left. + \frac{2(N_l^2 - 1) \sinh(A) - \sin(A)}{3 \cosh(A) + \cos(A)} \right] \\ &= 10.8 \times \left[ \frac{\sinh(2 \times 10.8) + \sin(2 \times 10.8)}{\cosh(2 \times 10.8) - \cos(2 \times 10.8)} \right. \\ &\quad \left. + \frac{2(3^2 - 1) \sinh(10.8) - \sin(10.8)}{3 \cosh(10.8) + \cos(10.8)} \right] \\ &= 64.6. \end{aligned} \quad (33)$$

The ac power loss is

$$\begin{aligned} P_{vac} &= F_R R_{wdc} (\gamma_r I_{dc}/2)^2 \\ &= 64.6 \times 33.9 \times 10^{-3} \\ &\quad \times (0.01 \times 0.807/2) (\text{W}) \\ &= 0.04 (\text{mW}), \end{aligned} \quad (34)$$

which is negligible compared with the dc winding loss because of a little ac component in the current through the inductor  $L_c$ .

The peak-to-peak value of the ac component of the flux density is

$$\begin{aligned} B_{pp} &= \frac{L_c \gamma_r I_{dc}}{N A_c} \\ &= \frac{1.33 \times 10^{-3} \times 0.01 \times 0.807}{46 \times 0.58 \times 10^{-4}} (\text{T}) = 4.02 \text{ mT}. \end{aligned} \quad (35)$$

The core power loss per unit volume is obtained from

$$P_v = a f^c (10 B_{pp}/2)^d, \quad (36)$$

where  $a$ ,  $c$ , and  $d$  are coefficients to calculate the core power loss provided by the core manufacturers. Additionally, for the Magnetics R ferrite material, these coefficients for  $f = 1 \text{ MHz}$  are  $a = 0.00806$ ,  $c = 1.66$ , and  $d = 2.68$ . Therefore, the core power loss  $P_c$  is obtained

$$\begin{aligned} P_c &= P_v V_c = a f^c (10 B_{pp}/2)^d V_c \\ &= 0.00806 \times (10^6)^{1.66} \\ &\quad \times (10 \times 4.02 \times 10^{-3}/2)^{2.68} \times 2.61 \times 10^{-3} (\text{W}) \\ &= 0.203 \text{ mW}. \end{aligned} \quad (37)$$

Total power loss of the inductor is

$$\begin{aligned} P_t &= P_{wdc} + P_{wac} + P_c \\ &= 50.2 + 0.04 + 0.203 = 50.4 \text{ mW} \end{aligned} \quad (38)$$

The equivalent series resistance (ESR) for the inductor is expressed as

$$\begin{aligned} R_{esr} &= \frac{P_t}{I_{dc}^2} \\ &= \frac{50.4 \times 10^{-3}}{0.807^2} (\Omega) = 62.5 \text{ m}\Omega. \end{aligned} \quad (39)$$

#### F. Confirmation of The Specified Conditions

From (6), the maximum flux density is calculated as

$$\begin{aligned} B_m &= \frac{LI_{dc}(1 + \gamma_r/2)}{NA_c} \\ &= \frac{1.33 \times 10^{-3} \times 0.807 \times (1 + 0.01/2)}{46 \times 0.58 \times 10^{-4}} \\ &= 0.404 \text{ T}, \end{aligned} \quad (40)$$

which is less than the saturated flux density  $B_{sat} = 0.5 \text{ T}$ , but 33 % larger than the specified value of  $B_m = 0.3 \text{ T}$ . This difference occurs due to the normalization of the air-gap length and the difference in the  $K_g$  value of the selected core. From this result, it can be stated that we should give the value of  $B_m$  with a sufficient margin from  $B_{sat}$ .

The ratio of the dc winding loss to output power is

$$\begin{aligned} \alpha &= \frac{P_t}{P_o} \\ &= \frac{62.5 \times 10^{-3}}{11.9} = 0.423 \%, \end{aligned} \quad (41)$$

which is 15 % lower than the required value because of the difference of the cross-sectional area of the wire and the  $K_g$  value.

The core window utilization factor is

$$\begin{aligned} K_u &= \frac{NA_w}{W_a} \\ &= \frac{46 \times 0.518 \times 10^{-6}}{0.6 \times 10^{-4}} = 0.397, \end{aligned} \quad (42)$$

which is almost the same as the required value. This is because we fix the number of turn  $N$  for adjusting the fringing effect.

Fundamentally, the design method using core geometry coefficient guarantees inductance value, maximum flux density, and ratio of the dc winding loss to output power as shown in Section II. However some differences appear due to air-gap length normalization, difference of selected wire size, and difference in the  $K_g$  value of the selected core.

### III. DISCUSSION OF RESULTS

The inductance value of the RF-choke inductor  $L_c$  of the class E switching circuit becomes small when the ripple ratio of the current through it becomes large. Small  $L_c$  value provides the small core volume  $V_c$  and a short length of the

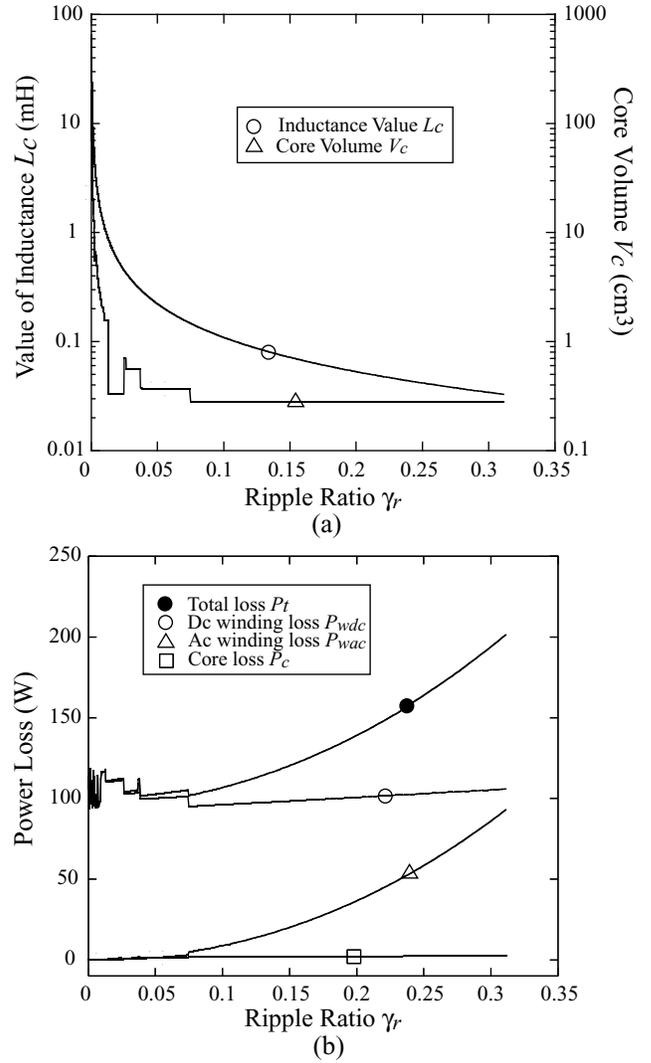


Fig. 2. Characteristics of the designed RF-choke inductor  $L_c$  as a function of the ripple ratio of the current  $\gamma_r$  for  $\alpha = 0.01$ ,  $I_{dc} = 0.807 \text{ A}$ , and  $f = 1 \text{ MHz}$ . (a) Inductance value  $L_c$  and core volume  $V_c$  of the designed inductor. (b) Dc winding losses  $P_{wdc}$ , ac winding loss  $P_{wac}$ , core loss  $P_c$ , and total power loss  $P_t$  of the designed inductor.

wire  $l_w$ . However, the increase of the ac component of the current make the large  $I_m$  and  $B_{pp}$ . Therefore, it is difficult to predict what happens in the inductor when the ripple ratio of the current varies. In this section, we investigate this problem. The all designed inductor in this section consists of Magnetics ferrite core from References [3] and [7] and AWG standardized wire.

Figure 2 shows the characteristics of the RF-choke inductor of the class E amplifier designed by  $K_g$  method as a function  $\gamma_r$ . For the design of the class E amplifier, the specifications, which are  $f = 1 \text{ MHz}$ ,  $V_{DD} = 15 \text{ V}$ , and  $R = 10 \Omega$ , are given. Additionally,  $\alpha = 0.01$ ,  $B_m = 0.3 \text{ T}$ , and  $J_{max} = 5 \text{ A/mm}^2$  are also given as specifications of the inductor design. Figure 2(a) shows the characteristics of the inductance value  $L_c$  and the

core volume  $V_c$ . As ripple ratio  $\gamma_r$  decreases, the inductance value increases. Because the high-inductance value prevent ac current from flowing through the inductor, high inductance value is necessary to generate the current with low ripple ratio. Therefore, the core volume  $V_c$  becomes large with the decrease in the ripple ratio  $\gamma_r$ . The core volume is constant when  $\gamma_r > 0.075$ . This is because this core volume is the smallest for all prepared cores. It is seen from Fig. 2(b) that the dc winding loss and core loss are almost constant regardless of  $\gamma_r$ . The concept of  $K_g$  method is to achieve the required dc winding loss. The output power is constant against the ripple ratio variation. Therefore, the dc winding loss is also constant for all the ripple ratio. The designer can achieve the required maximum flux density  $B_m$  by using  $K_g$  method. Therefore, the core loss is also constant regardless of  $\gamma_r$ , which is small enough to neglect. When the ripple ratio increases, the ac component of the current through the inductor also increases. Therefore, ac winding loss increases with the increase in the ripple ratio. For large  $\gamma_r$ , the ac winding loss is almost same as the dc winding loss. This means that it is important to consider the ac winding loss when the ripple ratio  $\gamma_r$  is high.

For  $\gamma_r > 0.32$ , we cannot design the inductor by using  $K_g$  method. In this range, the maximum current density is higher than  $J_m$ . This means that the cross-sectional area of the wire is too narrow. For avoiding this problem, we need to set a smaller value of  $\alpha$  because a small power loss requires a wide cross-sectional area of the wire. This process, however, is a nonsense. In this case, we should not use  $K_g$  method. This is because it is guaranteed that the dc winding loss is lower than the required power loss, and we do not need to consider dc winding loss. Namely, the  $A_p$  method should be used in this situation.

Figure 3 shows the characteristics of the RF-choke inductor of the class E amplifier designed by  $K_g$  method as a function of  $\alpha$ . In this case,  $L_c = 1.33$  mH,  $I_{dc} = 0.807$  A and  $\gamma_r = 0.01$  are fixed for any  $\alpha$ . When the cross sectional area of the wire is narrow, the dc winding loss becomes high. Therefore, the increase of  $\alpha$  tends to the narrow cross-sectional area of the wire. Therefore, the core volume  $V_c$  becomes small as the  $\alpha$  increases as shown in Fig. 3(a). Since the large  $\alpha$  allows the large dc-winding loss, the dc winding loss is proportional to the  $\alpha$  as shown in Fig. 3(b). Conversely, the variations of the ac winding and the core losses are very small compared with the variation of the dc winding loss because the  $I_m$  and  $B_m$  are fixed when the  $\alpha$  is changed. Strictly, the core loss becomes small with the increase in the  $\alpha$  since the core volume  $V_c$  becomes small. It is seen from Fig. 3(b), both the ac winding loss and the core loss are negligible for all  $\alpha$ . For  $\alpha > 0.078$ , we cannot the design the inductor by using  $K_g$  method. Because the cross-sectional area of the wire is too narrow, the current density problem occurs in this range.

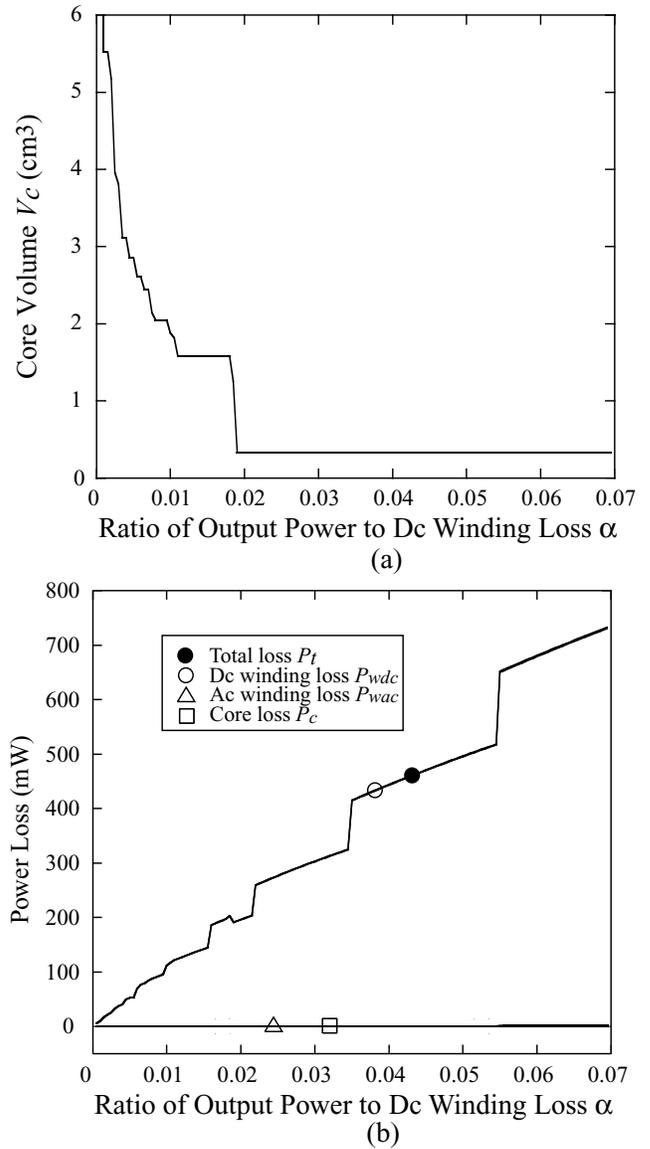


Fig. 3. Characteristics of the designed RF-choke inductor  $L_c$  as a function of the ratio of the output power to the dc winding loss  $\alpha$  for  $\gamma_r = 0.01$ ,  $I_{dc} = 0.807$  A, and  $f = 1$  MHz. (a) Core volume  $V_c$  of the designed inductor. (b) Dc winding losses  $P_{wdc}$ , ac winding loss  $P_{wac}$ , core loss  $P_c$ , and total power loss  $P_t$  of the designed inductor.

Figure 4 shows the characteristics of the RF-choke inductor of the class E amplifier designed by  $K_g$  method as a function of the  $I_{dc}$ . When we vary the dc-supply voltage  $V_{DD}$  of the class E amplifier, the output power  $P_o$  becomes high. The element values, however, do not vary when the dc-supply voltage  $V_{DD}$  varies. Therefore,  $L_c = 1.33$  mH,  $\gamma_r = 0.01$ , and  $\alpha = 0.01$  are fixed in Fig. 4. The maximum amplitude of the current  $I_m$  is high when the dc-current is high. For avoiding the maximum flux density  $B_m$  is larger than the saturated magnetic density  $B_{sat}$ , the core volume should be large with the increase in  $I_{dc}$  as shown in Fig. 4(a). The output power increases with the increase in  $I_{dc}$ , namely,  $V_{DD}$ . Because of

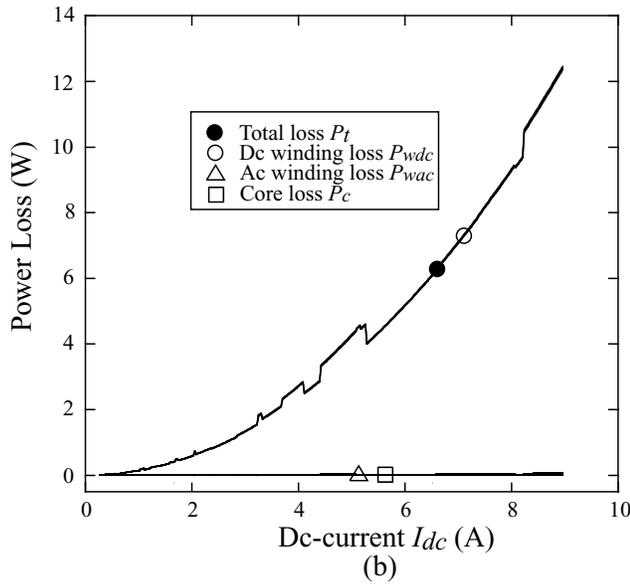
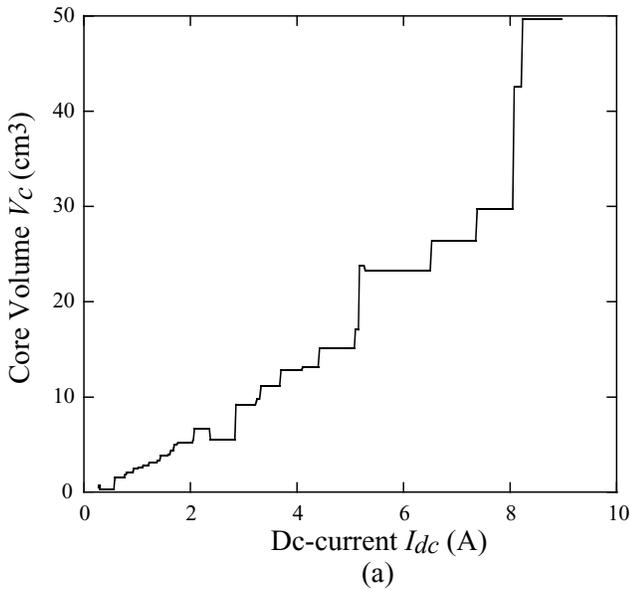


Fig. 4. Designed inductor characteristics of RF-choke inductor  $L_c$  as a function of the magnitude of dc current  $I_{dc}$  for  $\gamma_r = 0.01$ ,  $\alpha = 0.01$ , and  $f = 1$  MHz. (a) Core volume  $V_c$  of the designed inductor. (b) Dc winding losses  $P_{wdc}$ , ac winding loss  $P_{wac}$ , core loss  $P_c$ , and total power loss  $P_t$  of the designed inductor.

the fixed  $\alpha = 0.01$ , the dc winding loss, which is  $P_{wdc} = \alpha P_o$ , is also increases with the increase in  $I_{dc}$ . The dc winding loss is the dominant factor of the total power loss  $P_t$  as shown in Fig. 4(b), and the ac winding loss and the core loss are negligible. This figure shows the effectiveness to use the core geometry coefficient for the design of RF-choke inductors.

Figure 4 shows the characteristics of the RF-choke inductor of the class E amplifier designed by  $K_g$  method as a function of the operating frequency  $f$ . Dc-current through the inductor  $I_{dc}$ ,  $\gamma_r = 0.01$ , and  $\alpha = 0.01$  are fixed for all the designs

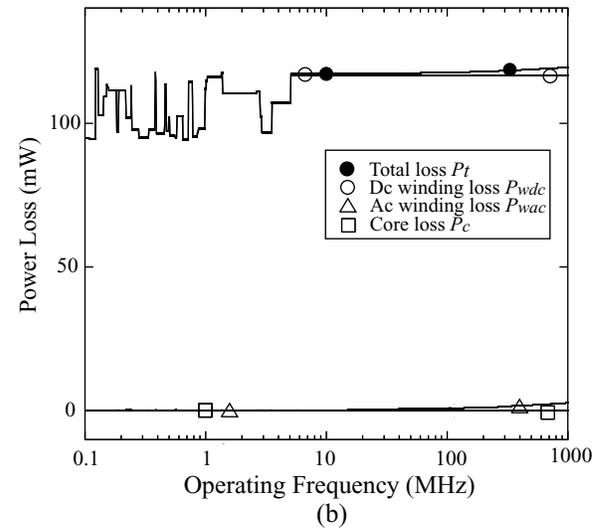
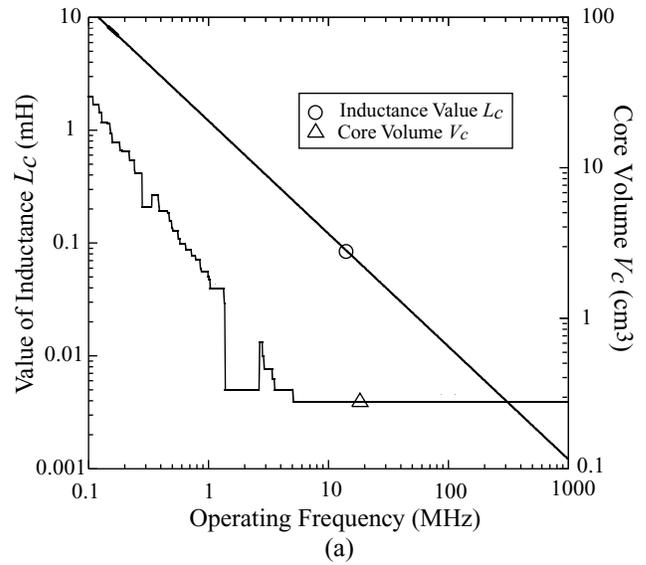


Fig. 5. Designed inductor characteristics of RF-choke inductor  $L_c$  as a function of the operating frequency  $f$  for  $\gamma_r = 0.01$ ,  $\alpha = 0.01$ , and  $I_{[dc]} = 0.807$  A. (a) Inductance value  $L_c$  and core volume  $V_c$  of the designed inductor. (b) Dc winding losses  $P_{wdc}$ , ac winding loss  $P_{wac}$ , core loss  $P_c$ , and total power loss  $P_t$  of the designed inductor.

of the inductors in this figure. A higher frequency makes the inductors be small. Therefore, the  $L_c$  decreases as increase of  $f$  as shown in Fig. 4(a). The core volume  $V_c$  also decreases. The designers should concern the core loss at high-frequency operations. The core loss for RF-choke inductor, however, generates low core loss as shown in Fig. 4(b). The ac-winding loss is also problem for high-frequency current because of the skin and proximity effects. It is seen from Fig. 4(c) that the ac-winding loss is also generated in RF-choke inductor. This is because the current has few ac component because of small  $\gamma_r$ . As a result, the dc-winding loss  $P_{wdc}$  is the dominant factor of the total loss  $P_t$  regardless of  $f$ . This result shows we can use ferrite core in spite of the high-frequency operations when

the RF-choke with low ripple-ratio current is designed.

#### IV. CONCLUSION

This paper has presented the fundamental theory to derive the  $K_g$  factor for the design of RF-choke inductor and design example. The design example indicates that the dc winding loss is dominant in the power losses of the RF-choke inductor. Fundamentally, it can be stated that the  $K_g$  method is useful for the design of RF-choke inductors because the required dc winding loss can be achieved. In some cases, however, the current density is a bottleneck for the design of the inductor. In the cases, the  $A_p$  method is better than the  $K_g$  method. This is because the coefficient of the  $A_p$  method takes into account the maximum current density instead of the dc winding loss.

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